Dispersion of metal-insulator-metal plasmon polaritons probed by cathodoluminescence imaging spectroscopy

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Cathodoluminescence imaging spectroscopy is used to excite and characterize the resonant modes of Fabry-Perot resonators for surface plasmon polaritons confined in a metal-insulator-metal (MIM) geometry. The smallest MIM plasmon wavelength derived from the observed mode pattern is found to be 160 nm in cavities with a 10 nm SiO₂ layer for a free-space wavelength of 645 nm. The measured wavelength agrees well with values from analytical dispersion relation calculations. Calculations of the excitation probability show that the resonant excitation of MIM plasmons depends strongly on the electron energy due to phase retardation effects resulting from the finite electron velocity.

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Surface plasmon polaritons (SPPs) are electromagnetic waves that propagate at the surface of a metal. Their evanescent field tail typically extends several hundreds of nanometers into the surrounding dielectric. Near the surface plasmon frequency, the SPP dispersion relation deviates strongly from the light line toward larger wave vectors, thus enabling short plasmon wavelengths at optical frequencies.

The dispersion relation of plasmons can be further tuned in metal-insulator-metal (MIM) geometries, in which the plasmon field is confined in a 10–100 nm dielectric gap between two metal layers. Due to intercoupling of plasmons at both metal-dielectric interfaces, plasmon modes with symmetric and antisymmetric magnetic field distribution exist, of which the latter shows the largest dispersion and highest loss. ^{2,3}

The unique properties of MIM plasmons are currently a research topic that attracts interest. The propagation of MIM modes was measured in slot waveguides⁴ and the dispersion relation was determined using near-field microscopy.⁵ Two-dimensional negative refraction of plasmons was demonstrated in the visible,⁶ and also confirmed theoretically.⁷ In these studies, MIM plasmons were excited by an external light source using in-coupling through slits in one of the metal cladding layers.

In this paper, we present cathodoluminescence (CL) spectroscopy measurements of MIM plasmon modes. We use the electron beam of a scanning electron microscope (SEM) that traverses through the layer stack to directly excite MIM plasmons confined in Fabry-Perot resonator structures. Measurements of the mode structure allow us to determine the MIM plasmon wave vector. A plasmon wavelength as small as 160 nm was found for a 10 nm SiO₂ layer. The observed wave vectors agree well with analytical calculations of the dispersion relation. Calculations of the excitation efficiency of MIM plasmons by an electron beam show the possibility of selective mode excitation.

The MIM samples were prepared using physical vapor deposition from a thermal evaporation source onto a cleaned

silicon substrate. The layer stack consisted of subsequent layers of 10 nm chromium, 100 nm silver, 10, 30, or 50 nm SiO_2 , 100 nm silver, and 10 nm chromium. A control sample was evaporated at the same time and shielded by a shutter during the SiO_2 evaporation leaving it without the SiO_2 layer.

The Cr layers were deposited to damp out single-interface SPPs propagating at the surface. Figure 1(c) shows the propagation length as a function of wavelength for the sym-

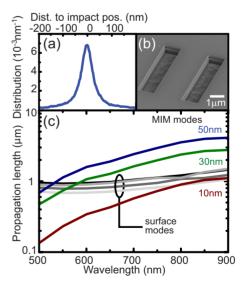


FIG. 1. (Color online) (a) Electron distribution as a function of position for 30 keV electrons in the center of the SiO_2 layer of the MIM structure along a direction perpendicular to the impinging beam. The electron distribution was calculated using a Monte-Carlo simulation. (b) SEM image of a one-dimensional Fabry-Perot resonator in a MIM structure. (c) Calculated propagation length as a function of wavelength for MIM and surface SPP modes for samples with 10, 30, or 50 nm SiO_2 layer and a silica-free control sample. The propagation lengths were calculated using a vectorial finite-difference mode solver.

metric MIM modes in comparison to the SPP mode propagating on the top interface, calculated using a vectorial finite-difference mode solver included in a commercial-simulation package. The propagation length for the top SPP modes varies only slightly depending on the underlying layer stack. For the longest wavelengths under consideration it is a factor of 3 lower than the propagation length for the MIM modes inside the 30 and 50 nm SiO₂ layers. Only for the 10 nm SiO₂ layer the propagation length of the Ag-surface mode exceeds the propagation length of the MIM mode. Note, that the asymmetric MIM mode, being in cut-off for the studied SiO₂ layer thicknesses, has 2–3 orders of magnitude shorter propagation lengths and will therefore not be observed.

The 30 keV Ga^+ beam of a focused ion-beam system was used to structure resonator structures into the MIM stack. The focused ion beam (beam current 48 nA) etched through the entire layer stack and approximately 200 nm into the underlying silicon substrate. Figure 1(b) shows an SEM image of a Fabry-Perot resonator structured into a layer stack with a 50 nm SiO_2 layer imaged under an angle of 52° off the surface normal. The one-dimensional cavity is formed by two parallel grooves of 1000 nm width that are spaced by a distance of 2000 nm. The groove length is 5000 nm. The Si substrate, the metal layers, and the SiO_2 can be easily identified. The contrast between Ag and Cr is too small to be seen in the image.

We use spatially resolved cathodoluminescence imaging spectroscopy⁹ to excite plasmon modes in the MIM structures and measure the emission in the far field. The samples are excited by the 30 keV electron beam of a SEM, which is focused to a 10 nm spot onto the sample surface. Due to electron scattering in the upper metal layers the beam diameter is increased as it penetrates into the layer stack. Figure 1(a) shows the result of a Monte-Carlo simulation 10 of the electron beam profile at the center of the SiO₂ layer, assuming a 10 nm diameter incident beam. The beam diameter is increased to approximately 50 nm. A parabolic mirror (acceptance angle 1.4 π sr) placed above the sample collects the emitted light and guides it to a spectrometer, in which the light is spectrally resolved and detected using a liquidnitrogen cooled charge-coupled device array. The collected spectra are corrected for system response by measuring the transition radiation spectrum for a known gold sample and normalizing it to the calculated transition radiation spectrum.9

Figure 2 shows the CL emission as a function of wavelength and electron-beam position for a line scan across three Fabry-Perot resonator structures: (a) the control sample without SiO₂ layer, (b) the MIM stack with a 50 nm SiO₂ layer, and (c) the stack with a 30 nm SiO₂ layer. In all three scans the grooves are clearly resolved at the top and bottom of the image as areas of low emission. The intensity is typically a factor of two higher if the beam is pointed onto the area between the grooves.

For the control sample in Fig. 2(a) a very weak periodic pattern of emission is observed between the grooves, which is symmetric around the center of the plateau. The amplitude of the oscillations decreases away from the grooves toward the center, and only a diffuse pattern is observed. The period

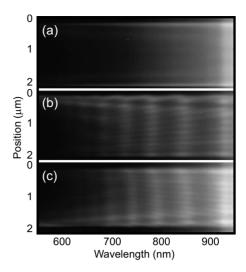


FIG. 2. Cathodoluminescence intensity as a function of position and wavelength for line scans across three $Ag/SiO_2/Ag$ MIM Fabry-Perot resonators with 2000 nm groove separation. Brighter colors indicate stronger CL emission. (a) Control sample without SiO_2 layer. (b) MIM structure with a 50 nm SiO_2 layer. (c) MIM structure with a 30 nm SiO_2 layer.

of the oscillations increases almost linearly with increasing wavelength and is approximately half the free-space wavelength.

The MIM sample with a 50 nm SiO_2 layer [Fig. 2(b)] shows a more intense oscillatory pattern. Seven bands of higher emission are observed for wavelengths of 610, 640, 680, 730, 780, 850, and 920 nm. The emission from the center of the resonator at these wavelengths shows oscillations with a period that is much shorter than the detected light wavelength. The amplitude and visibility of the oscillation fringes in each wavelength band strongly decrease for shorter wavelengths. Near the edges, a larger-period oscillation is superimposed comparable to the one in Fig. 2(a).

The MIM sample with a 30 nm SiO_2 layer [Fig. 2(c)] shows eight bands of high emission at 600, 630, 660, 695, 740, 790, 850, and 920 nm. The period of the oscillations for these wavelength bands is slightly shorter than for the 50 nm structure.

The observed CL emission of the measured samples stems from three sources that have to be taken into account: transition radiation (TR), radiation from SPPs propagating at the Ag/Cr interface, and radiation from MIM plasmons.

The TR contribution was determined by measuring the CL emission at a sample position where no structures are present that could scatter plasmons. The TR spectrum is very similar for all three samples, indicating that it is mainly determined by the uppermost layer.

First, we analyze the measurements of the control sample. The oscillations close to the grooves are attributed to interference of scattered SPPs with TR.⁹ The fact that only one oscillation is observed (rather than the extensive pattern in Ref. 9) is due to the fact that the propagation length of the surface SPPs is less than 1 μ m.

The MIM sample with the 50 nm SiO₂ layer also shows these oscillations near the edges, but in addition clear oscillations with a period much shorter than half the free-space

wavelength. We attribute these to Fabry-Perot modes of MIM plasmons that are reflected between the grooves.

To analyze the data, we have determined the period of the observed oscillations by fitting the CL intensity as a function of position x for each band with a function $\alpha \sin^2(k_{\text{MIM}}x)$, with $k_{\text{MIM}}=2\pi/\lambda_{\text{MIM}}$ the MIM plasmon wave vector. We find plasmon wavelengths of 330, 350, 370, and 430 nm for the light wavelength bands at 730, 780, 850, and 920 nm, respectively. For the bands at shorter wavelengths, the oscillations are damped out too strongly to allow us to fit their period. However, we can still derive the MIM plasmon wavelength for these bands from their mode number.

Each band of high emission in the CL scans corresponds to a cavity mode with a successive mode number n given by $2dk_{\text{MIM}}+\phi=2n\pi$ where d is the resonator width and ϕ is the phase change upon reflection (we assume $\phi=0$). For the above identified bands, we find mode numbers of n=9 (920 nm), n=10 (850 nm), n=11 (780 nm), and n=12 (730 nm). Therefore, the subsequent lower-wavelength bands should have mode numbers n=13 (680 nm), n=14 (640 nm), and n=15 (610 nm). Given the resonator width, we can then derive the corresponding MIM plasmons wavelength as 305, 285, and 266 nm.

The MIM sample with a 30 nm SiO₂ layer shows eight bands of high emission corresponding to eight modes of the Fabry-Perot resonator. The bands are more closely spaced, corresponding to a smaller free-spectral range, which is in agreement with the shorter plasmon wavelengths expected for this sample. The stronger damping of the plasmons in this sample compared to the 50 nm SiO₂ sample leads to a smaller oscillation amplitude. Due to the stronger damping only the oscillation period of the three longest-wavelength bands can be fitted for this sample. We find plasmon (free space) wavelengths of 320 nm (780 nm), 340 nm (850 nm), and 390 nm (920 nm) corresponding to mode numbers of n=12, n=11, and n=10, respectively. From the mode number the plasmon wavelengths for the other bands are derived to be 227 nm (600 nm), 240 nm (630 nm), 255 nm (660 nm), 272 nm (695 nm), and 280 nm (740 nm).

For the sample with a 10 nm SiO_2 layer, bright bands are observed at 645, 663, 680, 704, 734, 765, 805, 846, and 892 nm. Since the wavelength of the MIM plasmons is too short to resolve oscillations and fit their period, we have used the analytical dispersion relation to calculate the mode number n=17 for the band at 892 nm. From the subsequent mode numbers n=18-25 we derived the wave vectors for the higher-energy bands.

Figure 3 shows the MIM mode dispersion relation for the 10, 30, and 50 nm thick SiO₂ layers, with data points as derived above. The analytical dispersion relation for the symmetric MIM mode is also plotted, calculated from the optical constants for the layer stack measured using spectroscopic ellipsometry. The experimental data agree remarkably well with the calculation and lie far to the right of the light line in SiO₂, thus demonstrating the strongly dispersive character of these MIM modes. The good agreement between experiment and the calculated dispersion relation for symmetric MIM plasmons, confirms our assumption that the observed plasmon modes are of symmetric character.

To illustrate the excitation mechanism in our experiment,

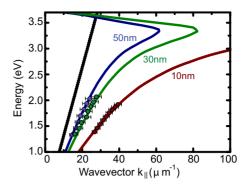


FIG. 3. (Color online) Dispersion relation for symmetric $Ag/SiO_2/Ag$ MIM plasmons with a 10 nm (red), 30 nm (green), and 50 nm SiO_2 layer (blue). The dots are derived from the cathodoluminescence line scans of Fig. 2. The solid lines are analytical calculations based on measured dielectric constants. The light line in SiO_2 is drawn in black.

we have investigated the excitation probability of MIM plasmons by an electron beam. For the studied MIM cavities the incident electron crosses the boundary between the metal and SiO_2 twice, generating excitations at both metal-dielectric interfaces. Due to the finite velocity of the electrons, the plasmon fields excited at the two interfaces will have a phase difference $\Delta\phi$ depending on the thickness d of the SiO_2 core and the electron velocity v:

$$\Delta \phi = 2\pi \frac{d}{v} \frac{c}{\lambda} + \phi_0, \tag{1}$$

where λ is the free-space wavelength. The phase factor ϕ_0 accounts for the phase difference between the plasmon fields generated at the electron transition from metal to dielectric and vice versa; for the MIM structure $\phi_0 = \pi$.

Figure 4(a) shows the calculated phase difference as a function of electron velocity at a free-space wavelength of 800 nm for three different SiO_2 layer thicknesses of 30, 50, and 100 nm. The phase difference increases inversely with decreasing electron velocity and linearly with layer thickness. The inset of Fig. 4 shows the schematic magnetic field profiles for the symmetric and antisymmetric MIM modes.

The phase difference leads to constructive or destructive interference between excitations on the two interfaces. The experimentally observed MIM modes are of symmetric character and have the highest-field intensity in the dielectric core as shown in the inset of Fig. 4(a). Therefore, we expect a decrease in emission probability for symmetric MIM plasmon at phase difference of $\Delta \phi = (2n+1)\pi$, with integer n [indicated by dashed lines in Fig. 4(a)].

At the marked positions, as well as in the limit of large v and small dielectric thickness a plasmon mode with antisymmetric magnetic field distribution (see inset of Fig. 4) will be preferentially excited. We attribute absence of these modes in our measurements to the fact that their propagation length is extremely short.³

The emission probability for the symmetric plasmon mode in an MIM cavity was calculated as described in Ref. 11. The results are shown in Fig. 4(b) as a function of electron velocity for SiO_2 layer thicknesses of 30, 50, and 100

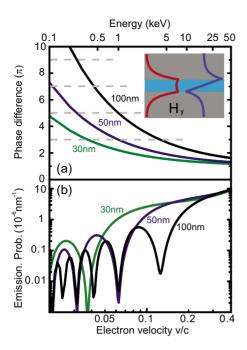


FIG. 4. (Color online) (a) Phase difference for plasmon excitation (free-space wavelength 800 nm) by an electron passing through a MIM structure as a function of electron velocity. The phase difference was calculated for an SiO_2 thickness of 30 nm (green), 50 nm (blue), and 100 nm (black line). The gray horizontal dashed lines denote phase differences of $(2n+1)\pi$ with integer n. Inset: Schematic of the magnetic field profile for the symmetric (red) and antisymmetric (blue) MIM mode. (b) Plasmon emission probability as a function of electron velocity for the symmetric MIM mode.

nm. We observe a decrease in the excitation rate with decreasing electron velocity, in agreement with higher localization of the external field produced by the electron. Superimposed on this decrease, we observe dips in the emission probability for electron velocities at which the phase difference equals an odd number times π . Moreover, the number of dips increases with layer thickness in agreement with Eq. (1).

These calculations indicate that it is possible to selectively

excite a plasmon mode with desired symmetry by varying the beam energy. For the studied samples, the dips of highest energy with reduced emission of symmetric MIM modes are found at very low-beam energies: 0.37 keV for the 30 nm SiO₂ layer (green curves) and 1.01 keV for the 50 nm SiO₂ layer (blue curves). For these energies the inelastic mean free path in Ag is very short (9 and 15 nm, respectively¹²) and the electron transmission through the upper Ag layer is thus extremely low. For a SiO₂ layer thickness of 100 nm, a dip of reduced emission is found for an energy of 4 keV. In this case the inelastic mean free path for the electron is 43 nm.

Due to the constraint of reduced electron transmission through the top Ag layer at low energies, it is difficult to experimentally demonstrate selective excitation of certain plasmon symmetry for normal-incidence electrons. However by tilting the sample with respect to the electron beam the path length d through the SiO_2 layer can be increased, so that selective excitation can be driven through the effective d rather than v in a modified version of Eq. (1). The fact that the excitation is generated at different lateral positions leads to an additional phase difference. The tilt required to achieve a minimum in symmetric mode excitation such as in Fig. d(b) for electrons incident on an MIM structure with a d(c) nm d(d) for electrons the sample has to be tilted to d(e).

We have shown that cathodoluminescence imaging can be used to excite and map plasmonic modes in Ag/SiO₂/Ag MIM structures. The generated MIM plasmons were confined in Fabry-Perot resonators. From the spatially resolved mode profile of the Fabry-Perot resonators the dispersion relation of the MIM plasmons was determined, and found to be in good agreement with theory. Additionally, we have shown that the excitation probability of resonant MIM plasmons depends strongly on the electron energy due to phase retardation effects resulting from the finite electron velocity.

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